

Beta Decay with Atom Traps

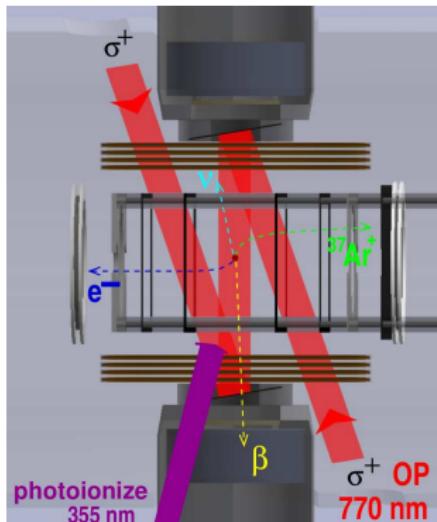
- In the decay of ^{37}K , we've made the most accurate measurement of the asymmetry of the β^+ direction with respect to the nuclear spin

Agrees with theory prediction
 Fenker et al. PRL 120 062502 (last week)

- Motivated by:
 Weak interaction changes within nuclei
 Left-right symmetric models.

4-fermi contact Lorentz ‘scalar’, ‘tensor’ from $A_{\beta}[E_{\beta}]$

- Plans with recoil progeny:
 A_{recoil} asymmetry of recoils
 Time-reversal violation in $\beta \nu \gamma$ decay
 $^{92}\text{Rb } E_{\nu}$ spectrum



TRIumf Neutral Atom Trap collaboration:

**S. Behling****B. Fenker**

M. Mehlman

P. Shidling

D. Melconian

A. Gorelov

J.A. Behr

M.R.

Pearson

[P. Kunz

J.Wong

L. Lambert]

Undergrad

A. Forestell

J. McNeilUNIVERSITY
OF MANITOBA**M. Anholm**

G. Gwinner

**D. Ashery****I. Cohen**

[TiC target chemists and 2 exhausted mortar/pestles]

Supported by NSERC, NRC through TRIUMF, Israel Science Foundation, DOE, State of Texas

 A_{β} is the Ph.D. thesis work of B. Fenker

Why the weak interaction is ‘weak’ at low energy

‘more massive virtual particles are created for shorter times’

Propagator+vertices:

$$T \propto \frac{G_X(-g^{\mu\nu} + p^\mu p^\nu / M_X^2) G_X}{p^2 - M_X^2} \quad p \ll M_X$$

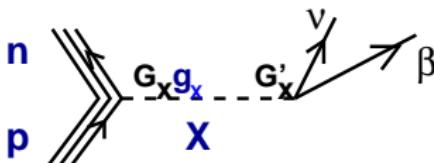
$$T \propto \frac{G_X^2}{M_X^2} \Rightarrow$$

- Decay rates $\propto \frac{G_X^2 G_X'^2}{M_X^4}$

or $\propto \frac{G^2}{M_W^2} \frac{G_X G_X'}{M_X^2}$ if process interferes with W
(couples to SM-handed ν)

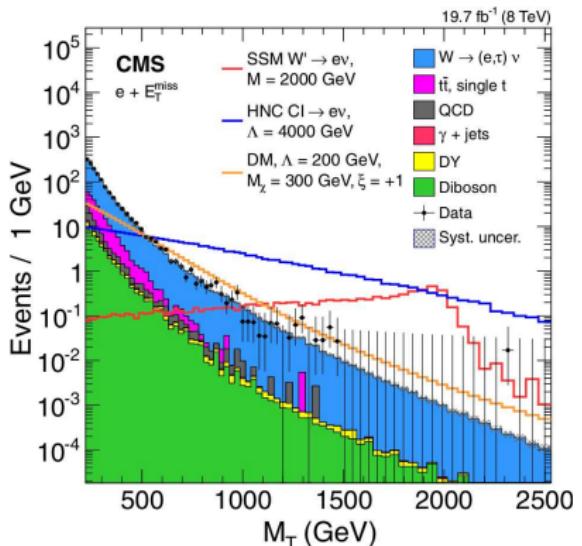
e.g. Fierz term $\propto \frac{m}{E_\beta}$

- IF $G_X \sim$ electroweak coupling, then 0.1% sensitivity in angular correlations $\rightarrow M_X \sim 6$ or **30 M_W**





Quasi-direct limits from high-energy colliders



Along with peak searches:
 LHC8 $\sigma[p + p \rightarrow e + \text{invisible}]$
 Just like $n \rightarrow p + e + \nu$
CMS PRD 91 92005
 Naviliat-Cuncic →
 Gonzalez-Alonso AnDP 2013
 (Cirigliano JHEP 2013)
 2 events expected, 1 seen
 (later Bhattacharya PRD 94
 054508 (2016) combined
 ATLAS, CMS.)

E.g. Left-Right symmetric models

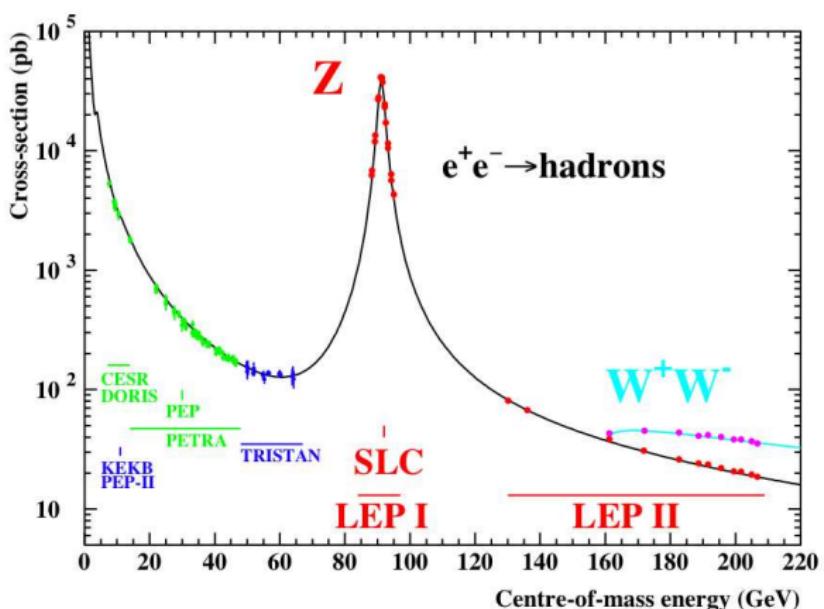
Extra W' with heavier mass, couples to ν_R

Otherwise same coupling strength, so parity is a good symmetry at very high energy

Renormalizable

Exchange bosons with lower m and smaller couplings?

Neutral exchange bosons can hide, but ‘weakly-coupled’ W still has electric charge



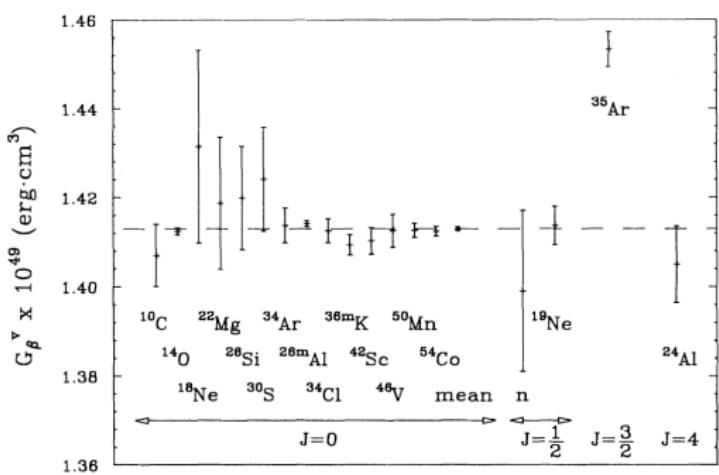
Does $e^+ + e^- \rightarrow W^+ + W^-$
cross-section
double for W?

Depends on the cut for W : typically this cut (explicitly listed in PDG) excludes low-mass W because of serious background



Weak interaction: same strength, all nuclei?

- Salam+Strathdee Nature 1974: phase transitions at very high B fields (10^{16} G) could drive $\theta_{\text{Cabibbo}} \rightarrow 0$ i.e. $V_{ud} \rightarrow 1$
- Suranyi+Hedinger PLB 56 151 1975: 10^{16} G possible in nuclei



Hardy+Towner PLB 1975:

$${}^{35}\text{Ar } A_{\beta} \leftrightarrow \theta_{\text{Cabibbo}} = 0$$

Adelberger, Fernandez,
Gossett, Osborne, Zeps

PRL 55 2129 (1985):
 $J=4$ ${}^{24}\text{Al} \leftrightarrow 0^+ \rightarrow 0^-$

Two more recent
measurements bring ${}^{35}\text{Ar}$
 A_{β} into agreement

FIG. 2. Measured values of G_{β}^V . The $0^+ \rightarrow 0^+$ values are inferred from Ref. 1. The $J = \frac{1}{2}$ and $J = \frac{3}{2}$ values are inferred from Refs. 3 and 4.

Suganuma+Tatsumi Ann.Phys. 208 407 (1991):
 10^{19} G breaks symmetry more

Parity Operation can be simulated by Spin Flip

Under Parity operation P :

$$\vec{r} \rightarrow -\vec{r} \quad \vec{p} \sim \frac{d\vec{r}}{dt} \rightarrow -\vec{p} \quad \vec{J} = \vec{r} \times \vec{p} \rightarrow +\vec{J}$$

The diagram illustrates the simulation of a parity operation (P) using a spin flip. It shows three stages of a particle's motion:

- Initial State:** Labeled 37K . A blue arrow points right, labeled v , and a purple arrow labeled β indicates the direction of motion.
- Intermediate State:** Labeled 37K . The blue arrow v has been reflected across the vertical axis, pointing left. A purple arrow labeled β indicates the direction of motion.
- Final State:** Labeled 37K . The blue arrow v has been reflected across the vertical axis again, pointing right. A purple arrow labeled β indicates the direction of motion.

A curved arrow between the second and third stages is labeled "180 rotation".

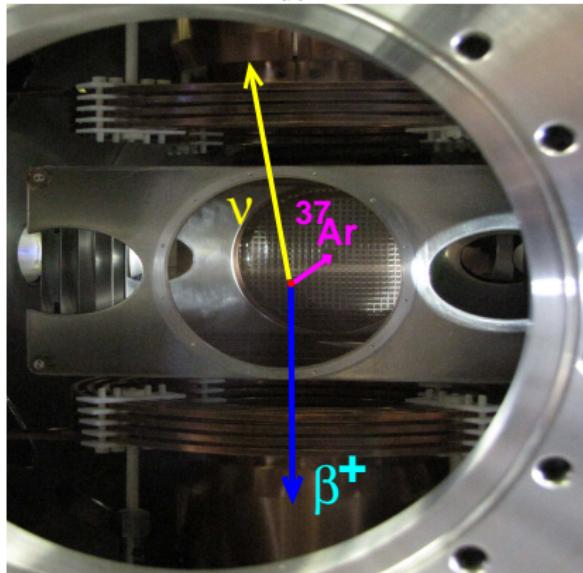
This is exact



3-momentum \vec{T} correlation

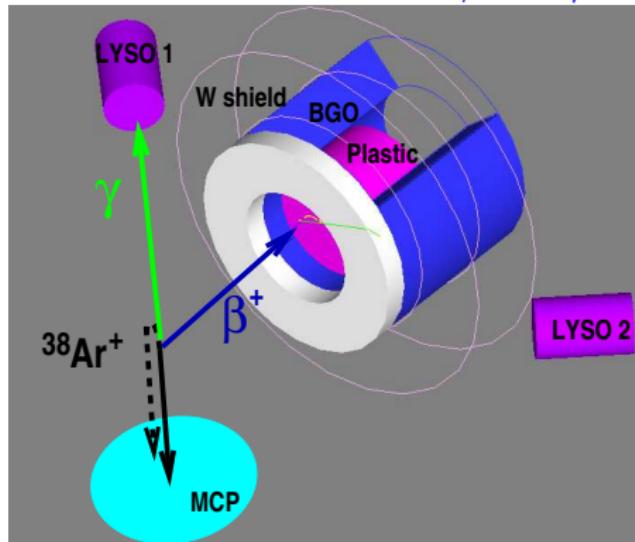
When $t \rightarrow -t$:

$$\vec{r} \rightarrow \vec{r} \quad \vec{p} \sim \frac{d\vec{r}}{dt} \rightarrow -\vec{p}$$



$$\vec{p}_{\nu} \cdot \vec{p}_{\beta} \times \vec{p}_{\gamma} = -\vec{p}_{\text{recoil}} \cdot \vec{p}_{\beta} \times \vec{p}_{\gamma}$$

$$\xrightarrow{t \rightarrow -t} \vec{p}_{\text{recoil}} \cdot \vec{p}_{\beta} \times \vec{p}_{\gamma}$$



BUT flipping t is not the same thing as running the decay backwards.

Particles interact on the way out, and you don't reverse that part.



One experimental discovery of parity violation

Wu, Ambler, Hayward, Hopper, Hobson, PR 105 (1957) 1413

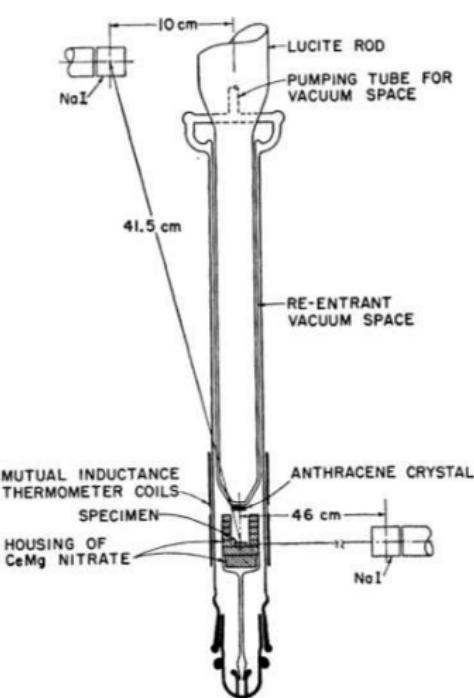
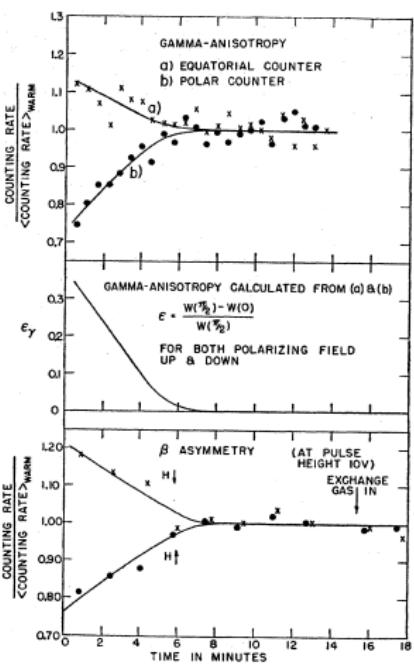
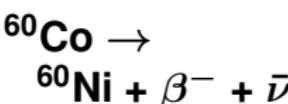


FIG. 2. Gamma anisotropy and beta asymmetry for polarizing field pointing up and pointing down.

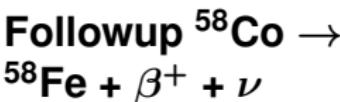
Dilution
Refrigerator
to spin-polarize



$$W[\theta] = 1 + PA\hat{I} \cdot \frac{\vec{p}_{\beta}}{E_{\beta}}$$

$$= 1 + A \frac{v}{c} \cos[\theta]$$

$$A_{\beta^-} \approx -1.0$$



$$A_{\beta^+} > 0$$

Wauters 2010 PRC $A_{^{60}\text{Co}} = -1.014 \pm 0.020$ [SM -0.987 ± 0.009]



^{37}K isobaric mirror decay: a ‘heavy neutron’ ?

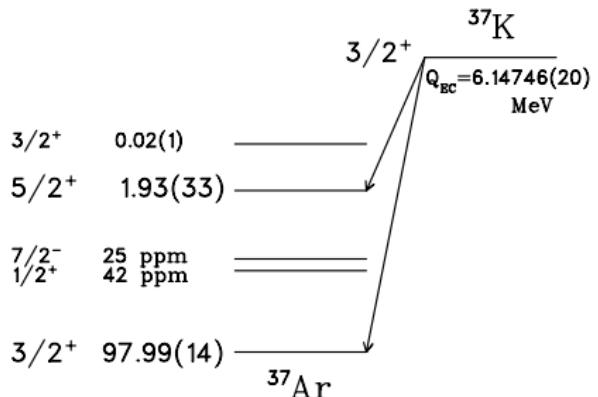
Here A_{β} isn't 1 or -1 or a clean fraction
there are 2 operators:

‘Fermi’ changes n to p

‘Gamow-Teller’ changes n to p and nucleon spin

τ , Q, and branch \Rightarrow decay strength $\mathcal{F}t$

We know the Fermi $\mathcal{F}t_0$ from the $0^+ \rightarrow 0^+$ decays, so from $\mathcal{F}t$ we can get the Gamow-Teller strength:



$\mathcal{F}t$ (Shidling PRC 2014) \Rightarrow

$$\rho = C_A M_{GT} / C_V M_F = 0.5768 \pm 0.0021$$

$$\Rightarrow A_{\beta}[\text{SM}] = -0.5706 \pm 0.0007$$

main uncertainty is experimental branching ratio



^{37}K isobaric mirror decay: a ‘heavy neutron’.

$$\Rightarrow A_{\beta}[\text{SM}] = -0.5706 \pm 0.0007$$

Dominant uncertainty is exp. branching ratio

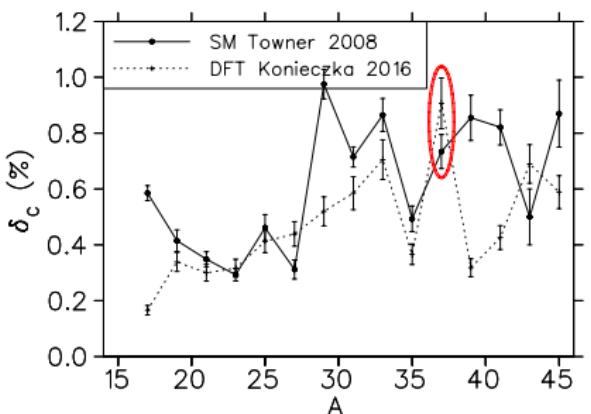
1st-order recoil-order from E&M moments:

Induced tensor $d_1 \approx 0$ for isobaric mirror

Small $\mu \Rightarrow$ small weak magnetism

Recoil-order + Coulomb + finite-size corrections \Rightarrow

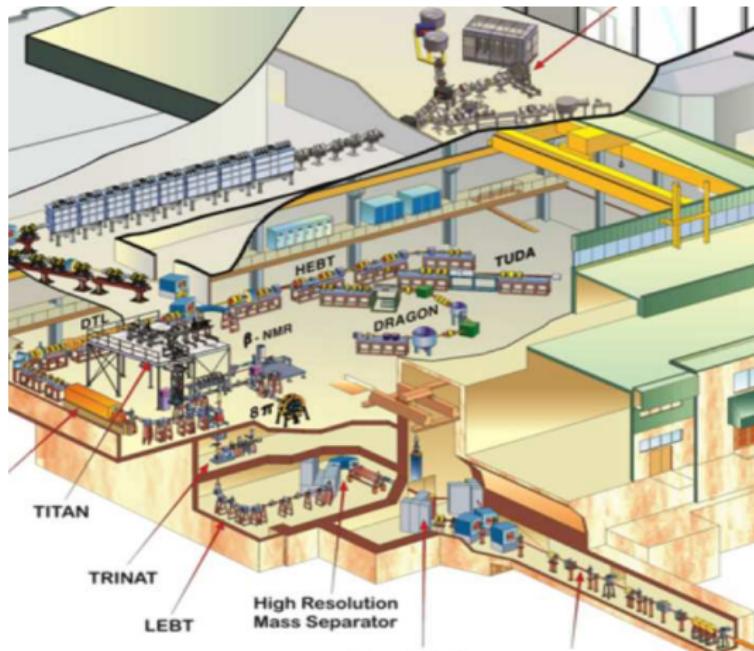
$$\Delta A_{\beta} \approx -0.0028 (E_{\beta}/E_0) \quad \text{Holstein RMP 1975}$$



Isospin mixing contributes 0.0004 uncertainty from shell model (10%)
 DFT for isospin mixing has improved functional for $A \sim 37$
 Using weighted average for δ_c would $\Rightarrow 0.0004 \rightarrow 0.0005$



TRIumf Neutral Atom trap at ISAC

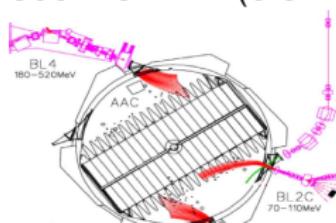


$^{37}\text{K } 8 \times 10^7/\text{s}$

TiC target
1750°C

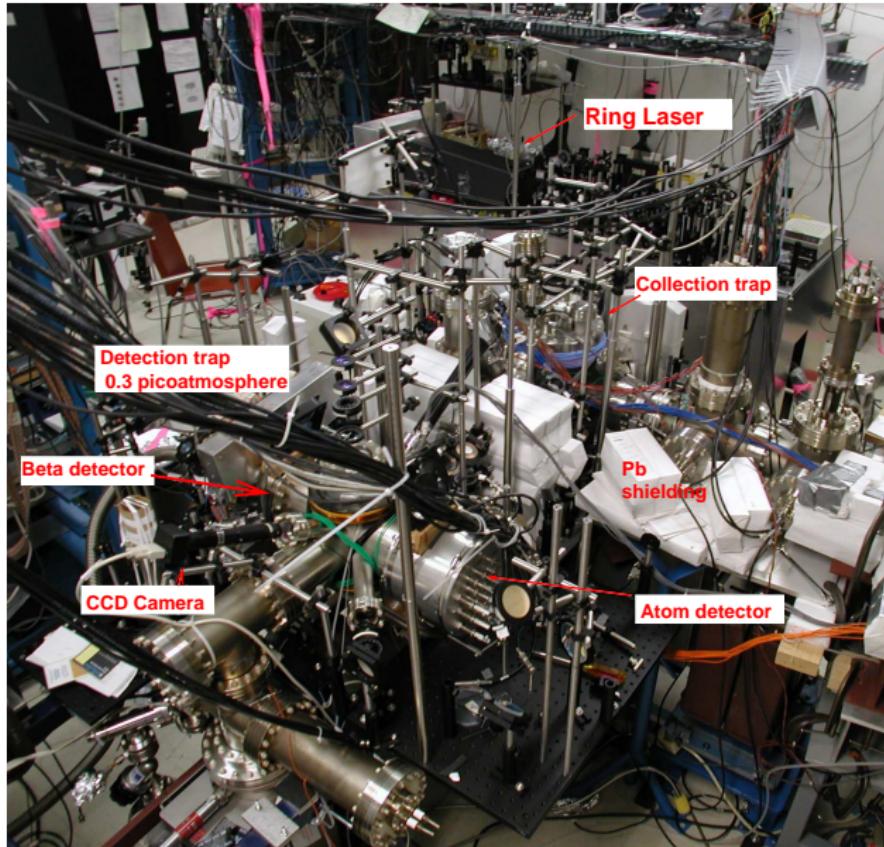
70 μA
protons

main TRIUMF cyclotron
'world's largest'
500 MeV H^- (0.5 Tesla)





TRINAT lab: “tabletop experiment”



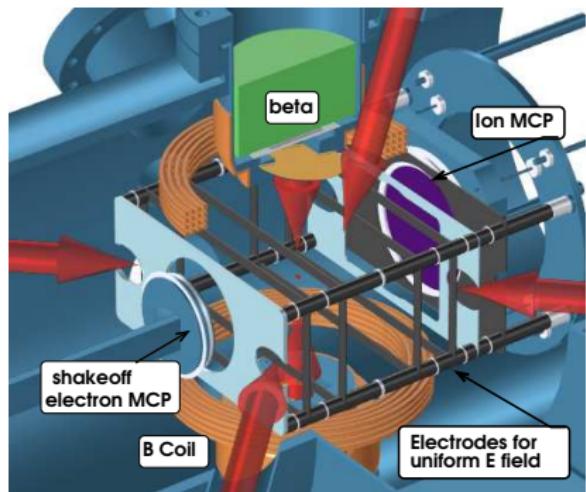
What elements can be laser cooled?

ICEPP Tokyo	$e+e^-$			
Raizen	H		CENPA ANL	He
	Li			Ne
Berkeley	Na	Mg		Ar
TRIUMF	K	Ca	Al	Kr
LANL, TRIUMF	Rb	Sr	Cr	Xe
LANL	Cs	Ba	Ag	
Stony Brook, JILA, Legnaro	Fr	Ra	Dy Er Yb	Hg

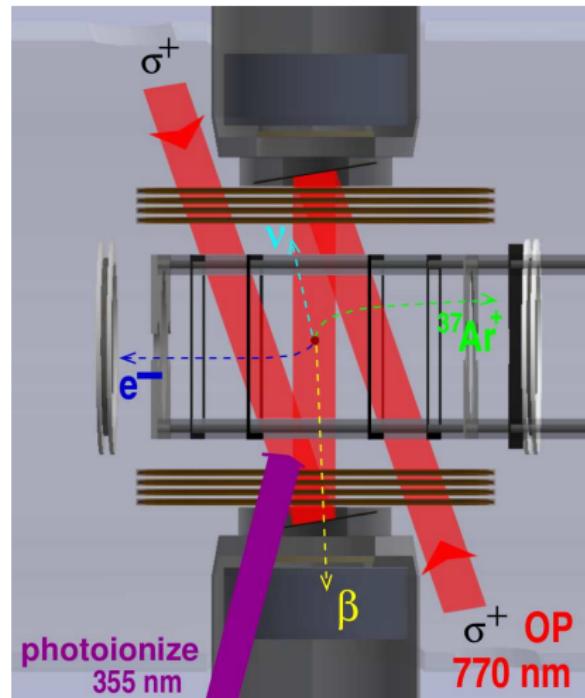
*Here Be
slain Dragons*



^{37}K decay geometry



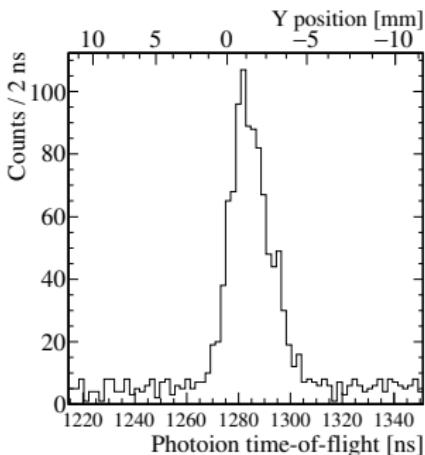
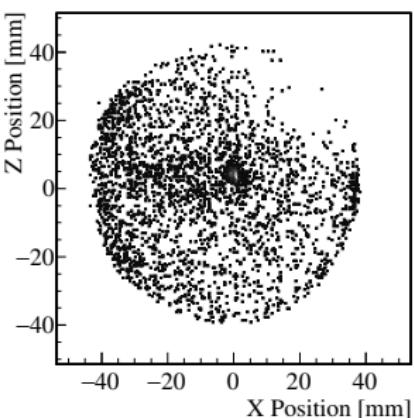
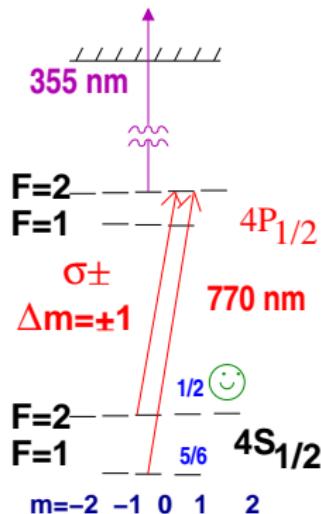
- β , recoil nucleus
- shakeoff e^- for TOF trigger



This decay pattern is helicity-forbidden if the ν goes straight up, independent of Gamow-Teller/Fermi ratio.



Optical pumping and probing ^{37}K

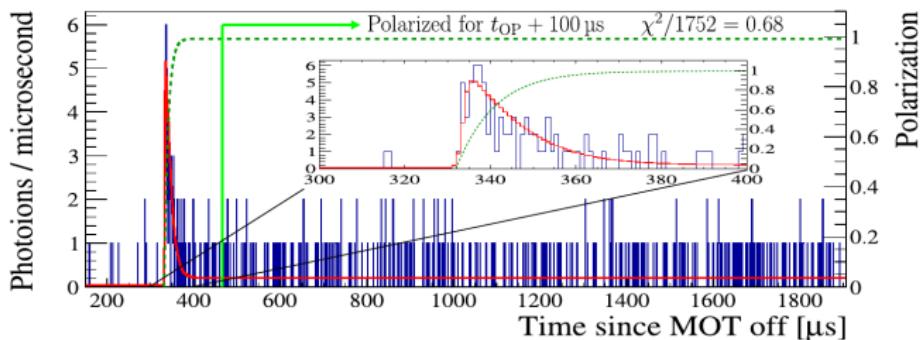


Photoionize 1%
in situ probe

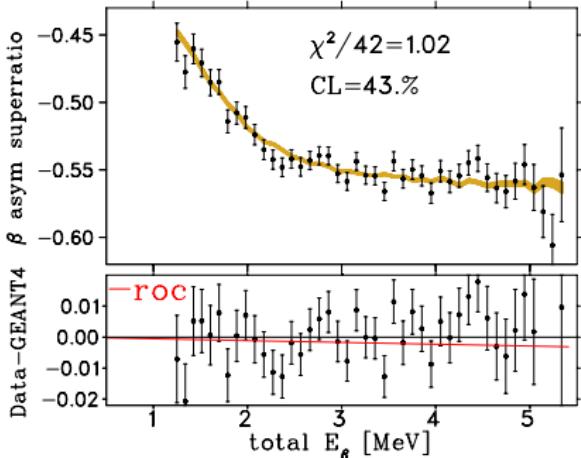
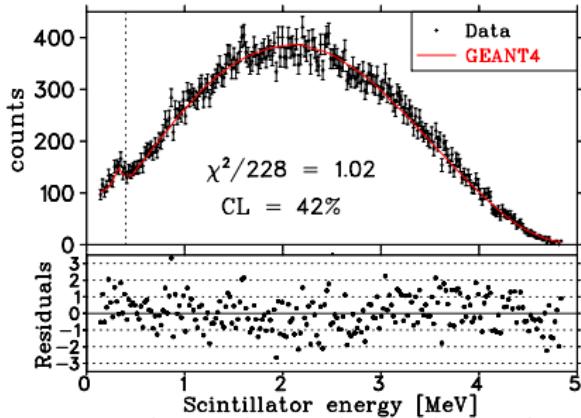
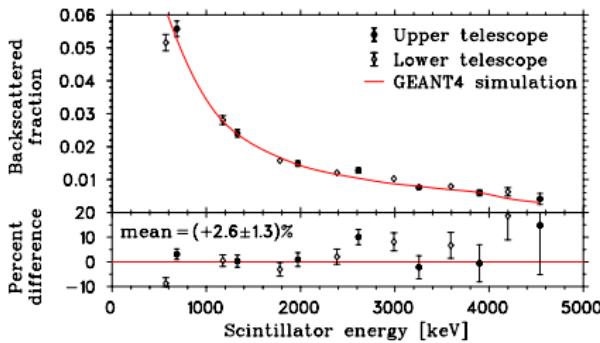
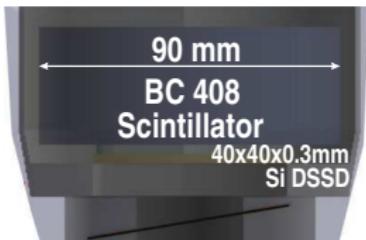
$$P_+ = +0.9913(8)$$

$$P_- = -0.9912(9)$$

Fenker NJP
2016



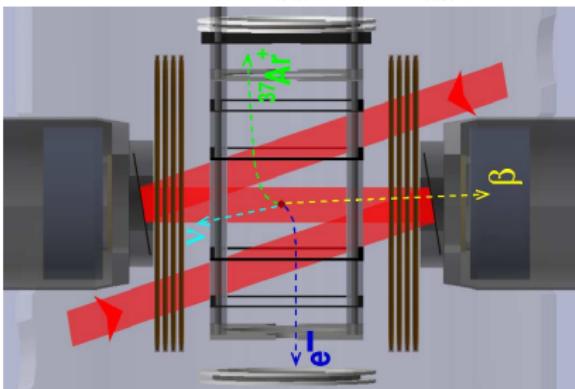
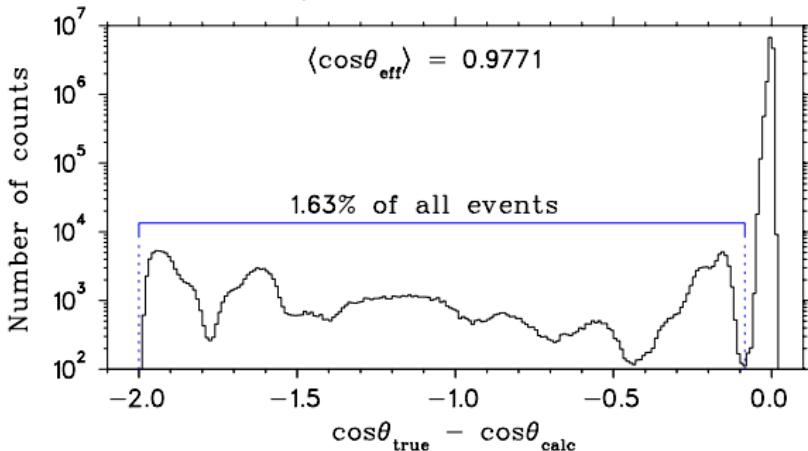
β^+ asymmetry ^{37}K data



- Backscatter from scint agrees to $\approx 5\%$ over E_{β^+} range of interest (in preparation)

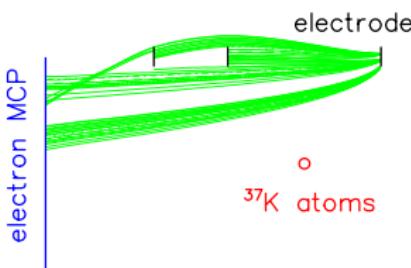
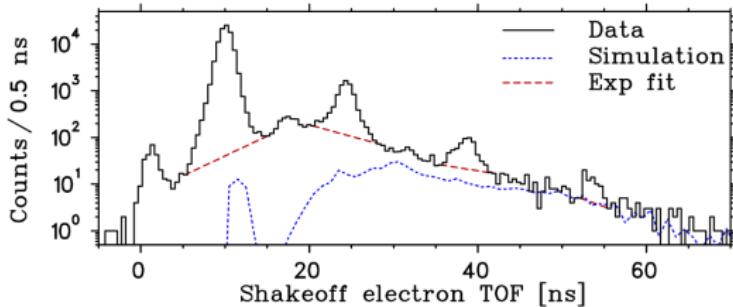


Scattered β 's





Background



- 2.8×10^{-3} of events in main peak are background from non-trapped atoms
- Conservatively assume polarized between 0 and 100%.
→ $A_{\beta} \times (1.0014 \pm 0.0014)$
- These will be removed by MCP position info when we increase to design E field

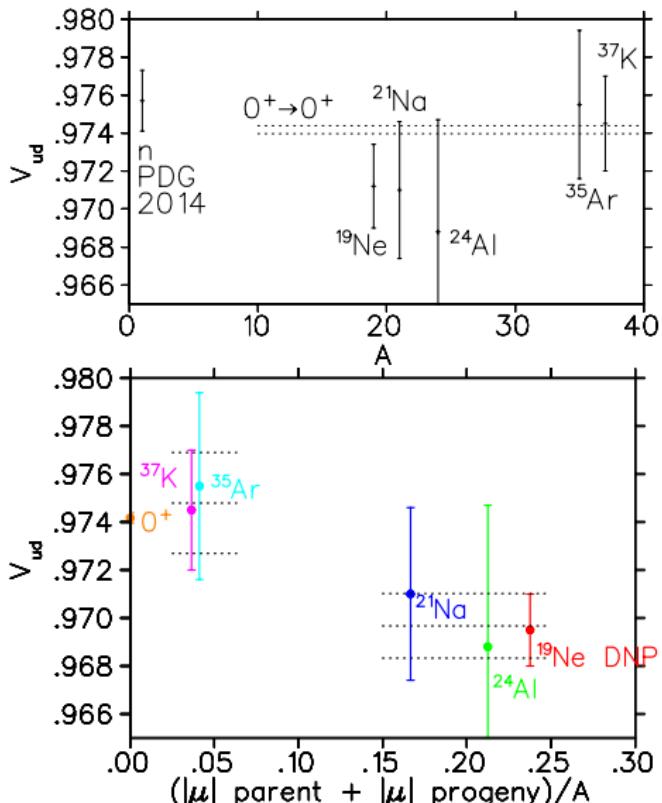
$^{37}\text{K } A_{\beta^+}$ Uncertainties



Source	Correction	Uncertainty	$A_{\beta} = -0.5707 \pm 0.0013 \text{ (stat)} \pm 0.0013 \text{ (syst)} \pm 0.0005 \text{ (pol)}$
Systematics			
Background	1.0014	0.0008	
β scattering ^a	1.0230	0.0007	
Trap (σ^+ vs σ^-)	position (typ $\lesssim \pm 20 \mu\text{m}$) sail velocity (typ $\lesssim \pm 30 \mu\text{m/ms}$) temperature (typ $\lesssim \pm 0.2 \text{ mK}$)	0.0004	
Si-strip	radius ^a ($15.5^{+3.5}_{-5.5} \text{ mm}$) energy agreement ($\pm 3\sigma \rightarrow \pm 5\sigma$) threshold (60 → 40 keV)	0.0005	
Shakeoff electron TOF region ($\pm 3.8 \rightarrow \pm 4.6 \text{ ns}$)		0.0001	
Thicknesses		0.0002	
Scintillator only vs. $E + \Delta E^a$	0.0001		
Scintillator threshold (400 → 1000 keV)	0.00003		
Scintillator calibration ($\pm 0.4 \text{ ch/keV}$)	0.00001		
Total systematics	0.0013		
Statistics	0.0013		
Polarization	1.0088	0.0005	
Total	1.0338	0.0019	

^aDenotes sources that are related to β^+ scattering.

Weak interaction: same strength, all nuclei?



$A_{\beta} \Rightarrow \text{GT/F}$

Then $\mathcal{F}t$ of $^{37}\text{K} \Rightarrow V_{ud}$

- An isospin mixing test useful for

$0^+ \rightarrow 0^+$ determination of V_{ud} i.e. $\psi[n] \neq \psi[p]$

- Salam and Strathdee Nature 1974:

phase transitions at very high B fields could drive $V_{ud} \rightarrow 1$

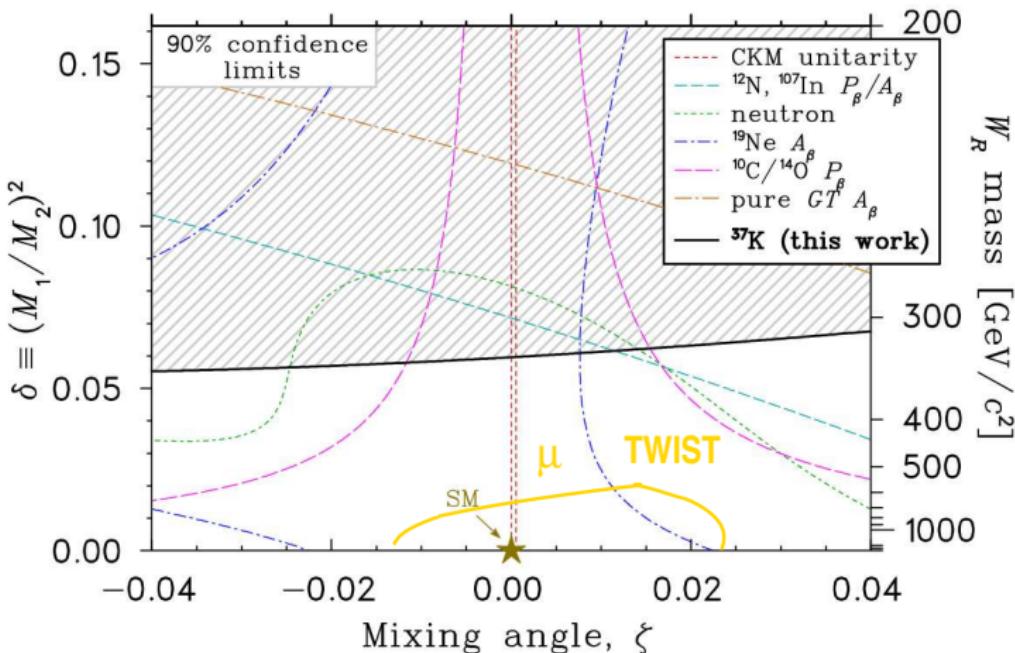
Hardy Towner PLB 1975 applied to the $^{35}\text{Ar } A_{\beta}$ controversy.

^{19}Ne Broussard DNP 2016

Left-Right Symmetric model

Extra W' with heavier mass, couples to ν_R

Otherwise same coupling strength, so parity is a good symmetry at very high energy



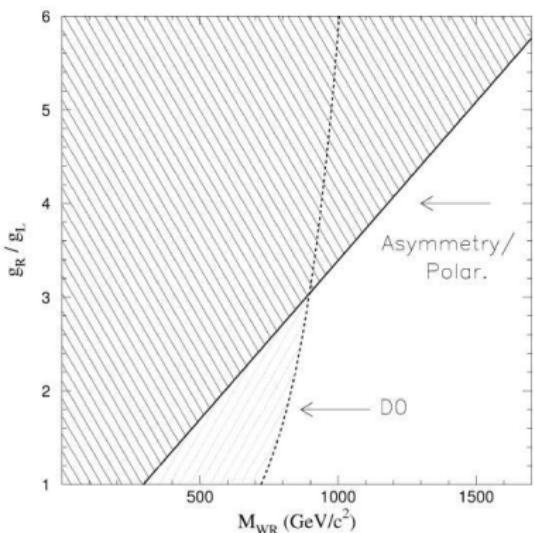
$^{37}\text{K}: M_W^R \wedge 352 \text{ GeV}$
90%

$(m[\nu_{\mu}^R] > m_{\mu})$ but LHC $M'_W > 3.7 \text{ TeV} 90\% \rightarrow$



'Non-manifest' Left-Right models

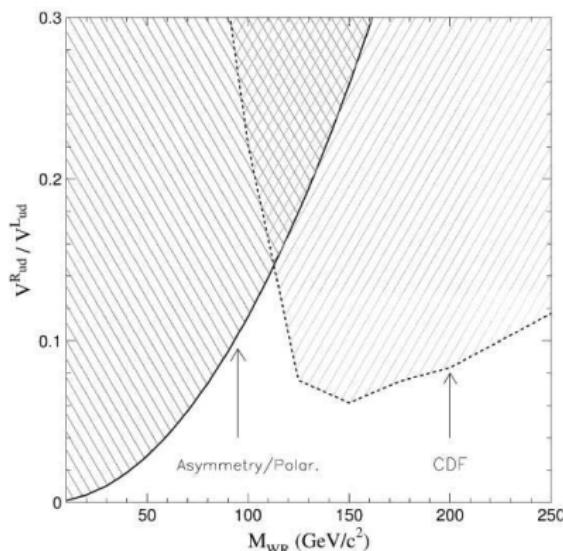
E. Thomas et al. / Nuclear Physics A 694 (2001) 559–589



$g_R > g_L$:

$^{37}\text{K} \Rightarrow g_R \lesssim 7.7$ at 4 TeV
(or $g_R < 4$, at 2 TeV but
LHC7 2 TeV 'bump' had
 $g \sim 0.5$)

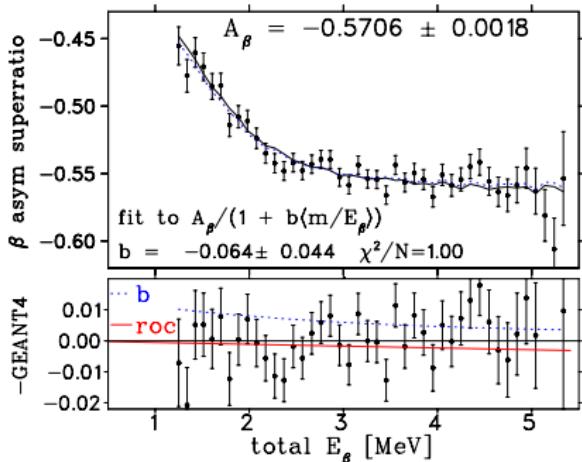
E. Thomas et al. / Nuclear Physics A 694 (2001) 559–589



$$V_{ud}^R < V_{ud}^L$$

For $M'_W < 70$ GeV, nuclear β decay constrains V_{ud}^R

PRELIM: $A_\beta [E_\beta]$ agrees with S.M.

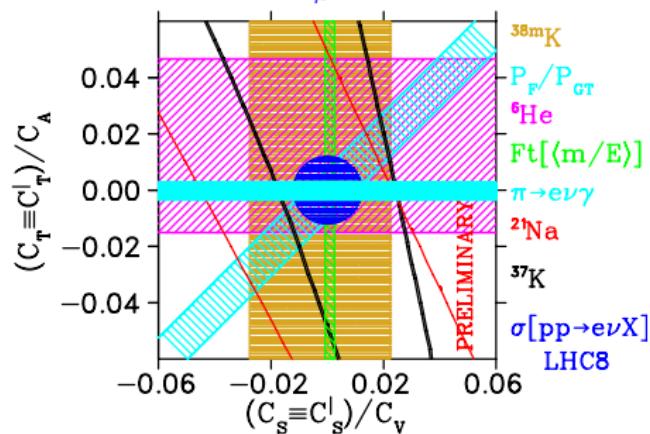


LHC8 $\sigma[p + p \rightarrow e\nu X]$
 Naviliat-Cuncic
 Gonzalez-Alonso AnDP 2013
 (Cirigliano JHEP 2013)
 1 event expected, 2 seen

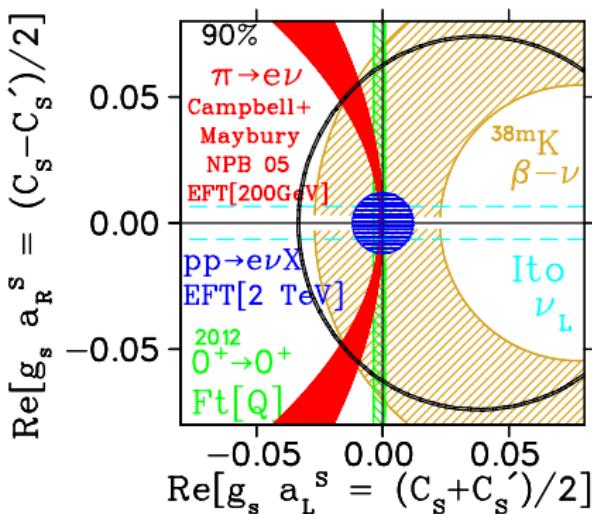
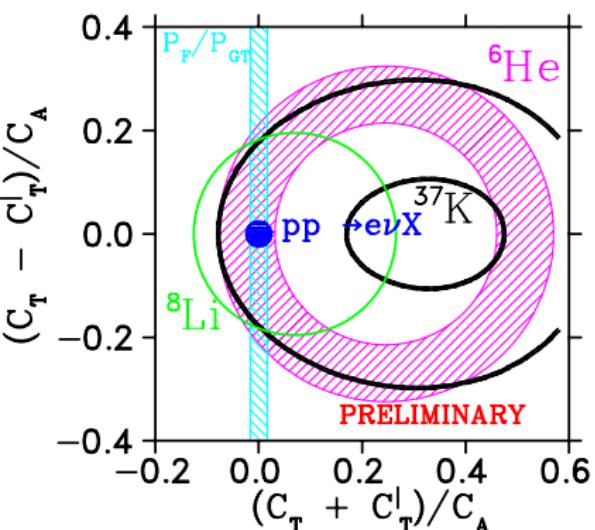
Specific models: leptoquarks $\rightarrow S, T$;
 Profumo 2007 PRD: MSUSY sum over sparticles $\rightarrow S, T$

Nucleon, Lepton Currents making up Lagrangian (a scalar) can separately transform like S, T, V, A
 1957 version of EFT.

Fierz term $\propto \langle \frac{m_\beta}{E_\beta} \rangle$



Couplings to wrong-handed ν



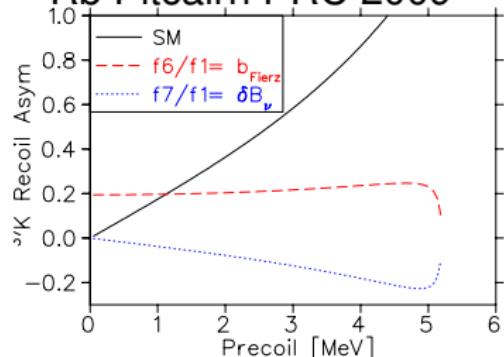
the Fierz term is ‘easier’ to constrain but has more competition

For scalars coupling to wrong-chirality ν , we compete with our own $^{38\text{mK}} \beta\nu$ Gorelov 2005

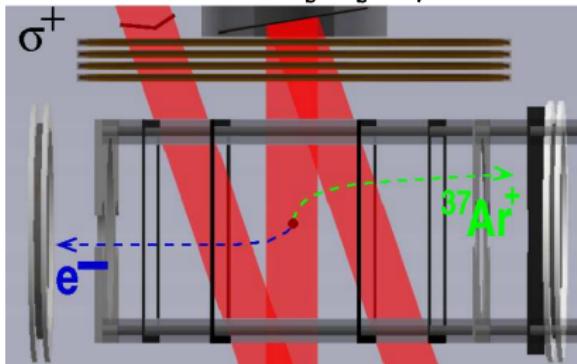
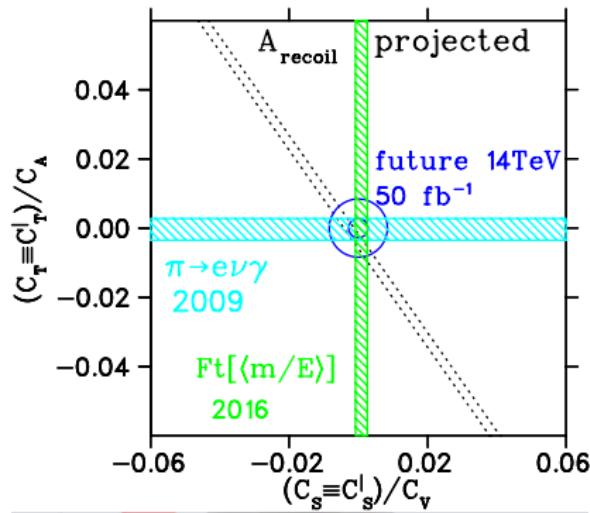
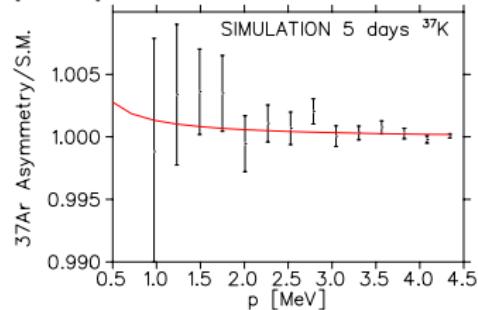


future $A_{\text{recoil}} \propto A_{\beta} + B_{\nu}$

Technique demonstrated in
 ^{80}Rb Pitcairn PRC 2009



Ave A_{recoil} depends on ρ ;
 ρ dependence doesn't




 $\gamma\beta\nu\chi$ Experiment

Harvey Hill Hill PRL 99 261601

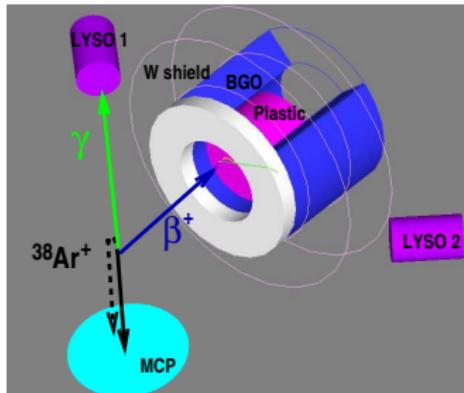
combine QCD+electroweak
interaction in the nucleon's \mathcal{L} , and
Gardner, He PRD 87 116012 (2013)

reduce this to $\mathcal{L} =$

$$-\frac{4c_5}{m_{\text{nucleon}}^2} \frac{e G_F V_{ud}}{\sqrt{2}} \epsilon^{\sigma\mu\nu\rho} \bar{p} \gamma_\sigma n \bar{\psi}_{eL} \gamma_\mu \psi_{\nu L} F_{\nu\rho}$$

which upon interference with S.M.
gives χ decay contribution →

$$|\mathcal{M}_{c5}|^2 \propto \frac{\text{Im}(c_5 g_V)}{M^2} \frac{E_e}{p_e k} (\vec{p}_e \times \vec{k}_\gamma) \cdot \vec{p}_\nu$$

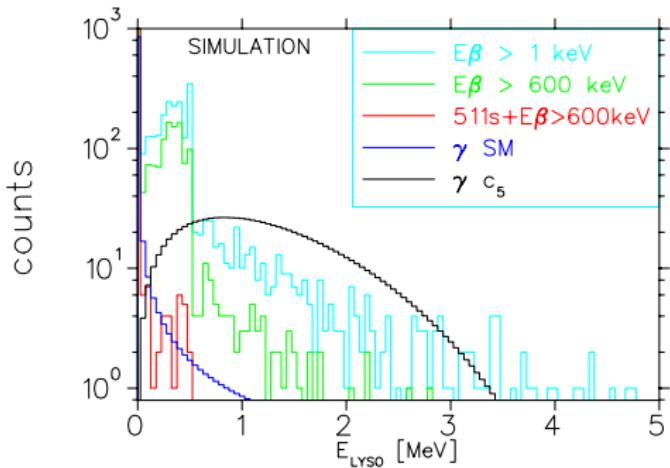
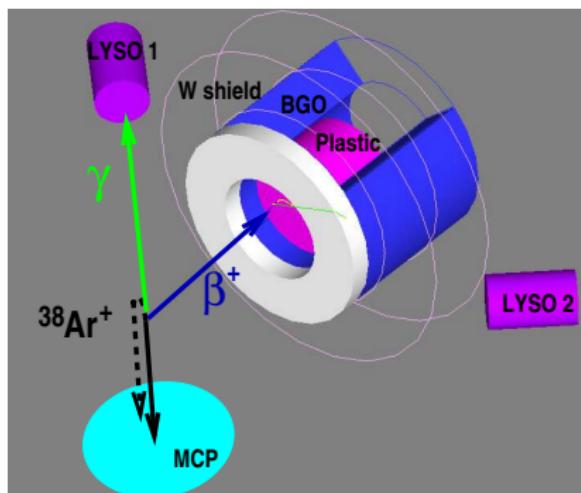


new physics $M \sim \text{MeV}$

- χ 250x larger in ^{38m}K decay than n
- final state fake effect 8×10^{-4}
- ^{38m}K 40,000 atoms, 30000 events/week ⇒ $\sigma \sim 0.02$
- Test asymmetry of apparatus with coincidence pairs
- n → p $\beta\nu\gamma$ branch (Nico Nature 06, Bales PRL 16) ⇒ $\frac{\text{Im}(c_5)}{M^2} \leq 8 \text{ MeV}^{-2}$ ⇒ Asym can be 100%

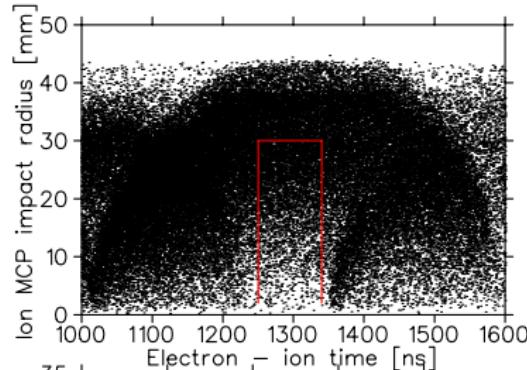
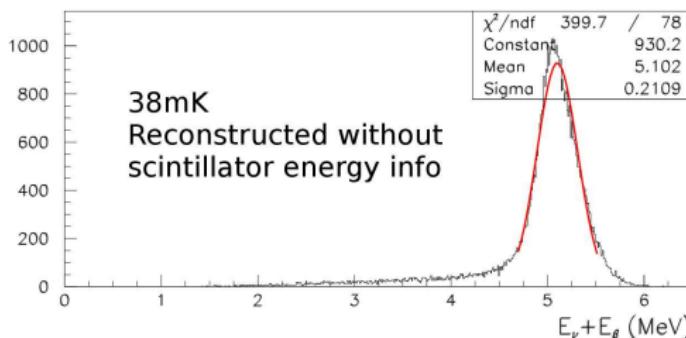
GEANT4 simulation of $\gamma\beta\nu\text{X}$

- the new ‘c5’ term needs Fermi or Fermi+GT transition $\Rightarrow \beta^+$ emitters
- background from β ‘external bremsstrahlung’ suppressed by requiring β^+ to hit plastic
- Require two 511’s in BGO, so we know they didn’t go to γ detector, enables measurements at $E_{\gamma} < 0.2 \text{ MeV}$.

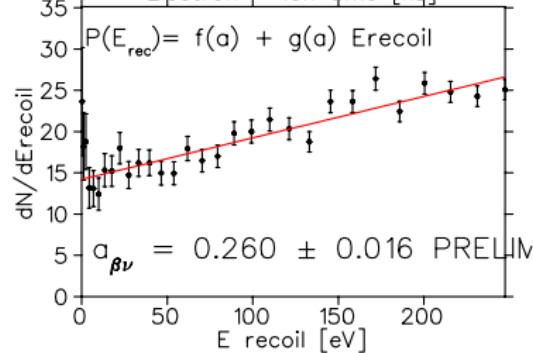


Reactor $\bar{\nu}$'s from $0^- \rightarrow 0^+$ ^{92}Rb decay

^{92}Rb produces $\sim 10\%$ of reactor $\bar{\nu}$'s from 5-7 MeV, important for possible sterile ν and for non-proliferation.



- Isolate and measure g.s. branch (3 exps have settled on $\sim 90\%$)
- Reconstruct the E_{ν} spectrum. (4 $0^- \rightarrow 0^+$ exps disagree.) Such decays make 1/3 of the 5-7 MeV reactor $\bar{\nu}$'s)
- $a_{\beta\nu}$ too far from 1 to look for pseudoscalar interaction →



TRIUMF Neutral Atom Trap: Near Future

We have measured the β asymmetry of ^{37}K decay to be $A_{\beta} = -0.5707 \pm 0.0019$

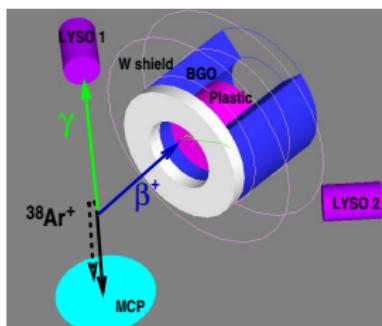
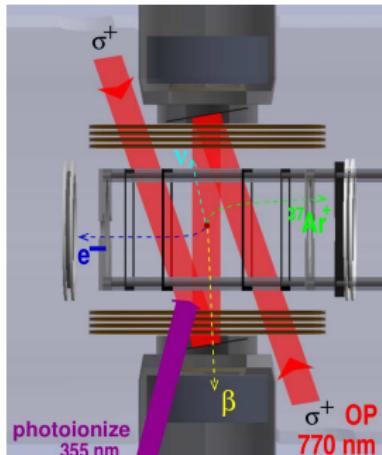
Agrees with theory -0.5706 ± 0.0007 , complements the best β decay measurements

Plans: measure $A_{\beta}[E_{\beta}]$ 3-5 x better

- A_{recoil} with sensitivity to '4-fermion contact' interactions complementary to $\pi \rightarrow e\nu\gamma$, $\pi \rightarrow e\nu$, and LHC $p + p \rightarrow e + E_{\perp}$

- A TRV $\beta\nu\gamma$ 3-momentum correlation, first of its type in 1st-generation particles

- $^{92}\text{Rb } 0^- \rightarrow 0^+ E_{\nu}$ spectrum





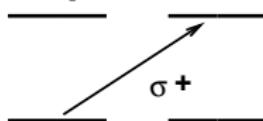
How to spin-polarize a nucleus with a laser: Part I

Polarize atom by Direct Optical Pumping

Biased random walk

Simple example:

$$J' = 1/2$$

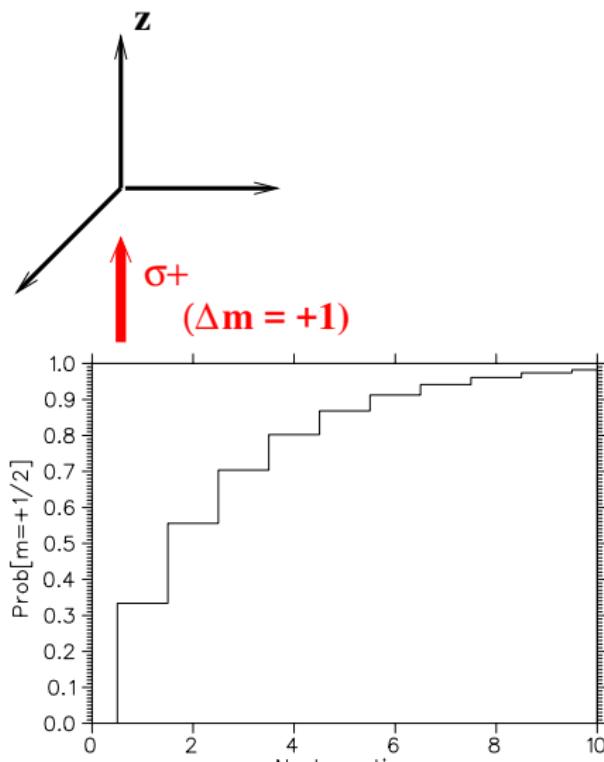


$$J = 1/2$$

$$m_J = -1/2 \quad m_J = +1/2$$

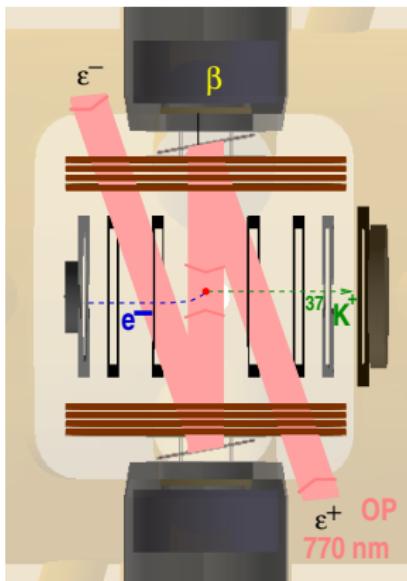
$P(m=1/2) = 1 - (2/3)^N$ after N steps

Need 12 photons absorbed to get to 99% of maximum.

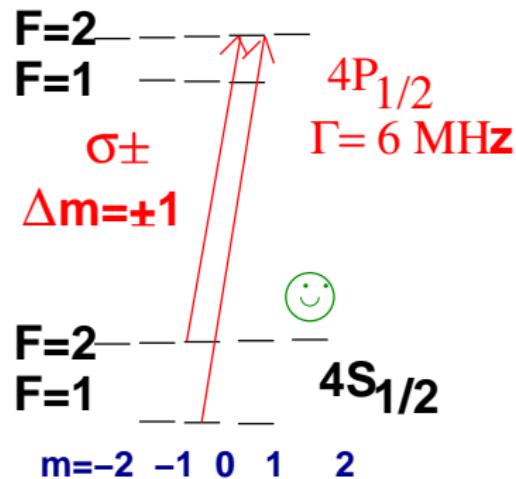




Direct Optical Pumping, $I=3/2$

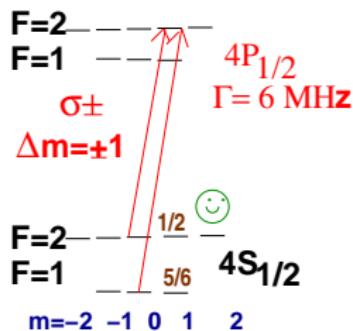


- Biased random walk
- σ^{\pm} light
- $4S_{1/2} \rightarrow 4P_{1/2}$ transition



- optimize with ^{41}K , almost same hyperfine splitting as ^{37}K
- $$\vec{F} = \vec{J}_{\text{atom}} + \vec{I}_{\text{nucleus}} \quad H_{\text{hyperfine}} = -\mu_N \cdot \vec{B}_e = A \vec{I} \cdot \vec{J}$$
- Spin flips: $\sigma^+ \rightarrow \sigma^-$;
small frequency shift (-2 MHz) to compensate Zeeman shift

TRIUMF Quantifying Polarization from excited state population



Tail \sim few % of peak \Rightarrow We need tail/peak to $\sim 10\%$ accuracy to extract P to $\sim 0.1\%$

We can't quite extract P by inspection:
 $\Delta F = 0$ for Larmor precession

Same centroid P from 2 approaches:

Rate eqs for classical populations

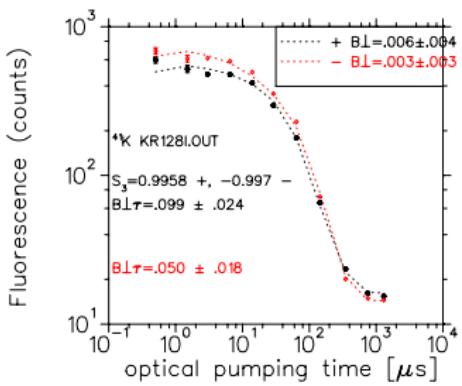
$$\frac{dN_i}{dt} = -R_{ji}N_i + R_{ij}N_j + \lambda N_j$$

Optical Bloch Eqs include B_{\perp} rigorously

$$\frac{d\rho}{dt} = \frac{1}{i\hbar} [\mathbf{H}, \rho] + \lambda$$

We measure S_3 and float B_{\perp}

($S_3 = -0.9958(8)$, $-0.9984(13)$,
 $+0.9893(14)$, $+0.9994(5)$)



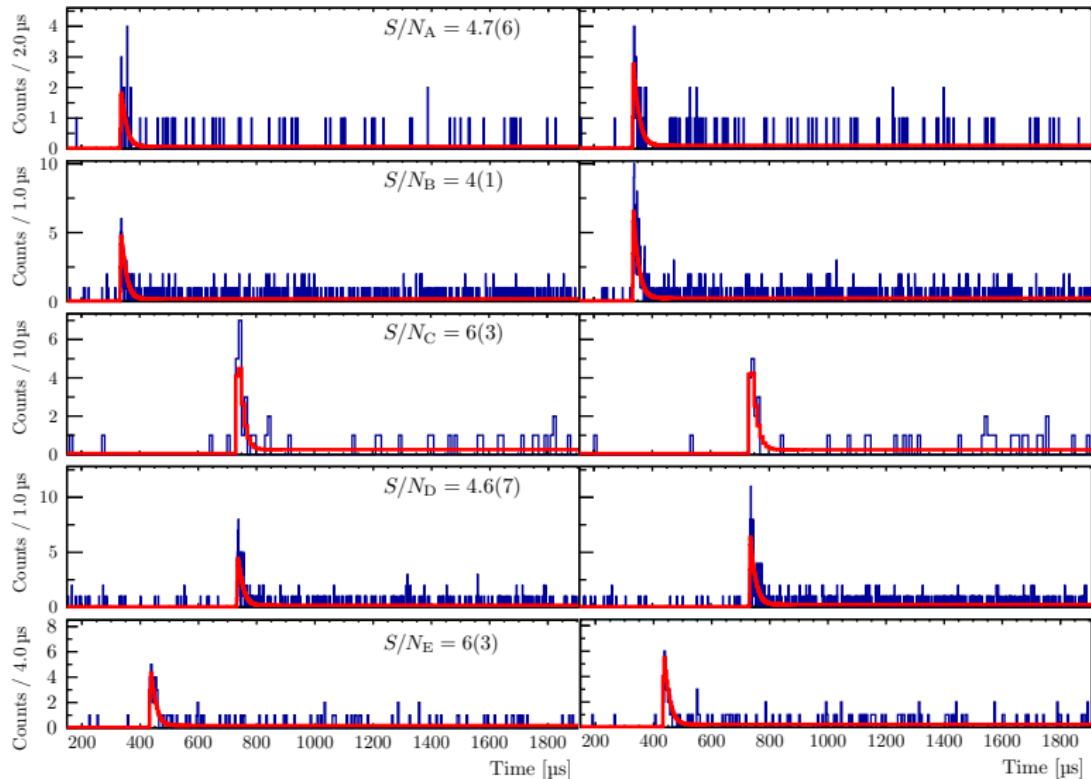


Polarization fit to all ^{37}K data

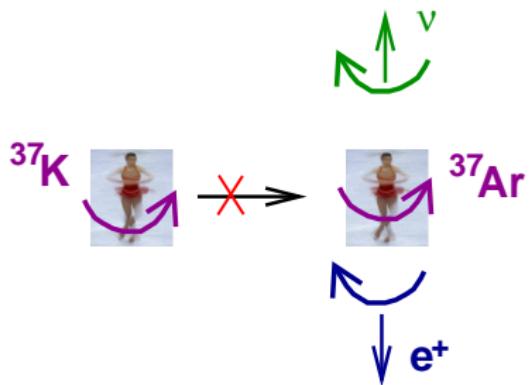
Transverse field (B_x) common to all: 124(8) mG

σ^- Polarization State

σ^+ Polarization State



Lepton helicity \rightarrow angular distribution



← This decay pattern needs
non-S.M. chirality

$I=3/2 \rightarrow I=3/2$:
Leptons can't increase
nuclear spin any further


Polarization Improvements
SYST $\times 10^{-4}$ ΔP ΔT Initial T $\sigma^- \quad \sigma^+$

Global fit v. ave

 $\sigma^- \quad \sigma^+$ S_3^{out} Uncertainty $\sigma^- \quad \sigma^+$

Cloud temp

 $\sigma^- \quad \sigma^+$

Binning

 $\sigma^- \quad \sigma^+$ B_z Uncertainty $\sigma^- \quad \sigma^+$ Initial P $\sigma^- \quad \sigma^+$ Require $I_+ = I_-$ $\sigma^- \quad \sigma^+$

Total SYSTEMATIC

 $\sigma^- \quad \sigma^+$

STATISTICS

 $\sigma^- \quad \sigma^+$ B. Fenker New J. Phys **18** 073028

2016

$$\begin{aligned} P(\sigma^+) &= +0.9913(8) & T(\sigma^+) &= -0.9770(22) & \bullet \text{Uncertainty} &\propto \\ P(\sigma^-) &= -0.9912(9) & T(\sigma^-) &= -0.9761(27) & (1-P) \end{aligned}$$

- pellicle mirrors: less β^+ scattering

- define T by OP
- trim B gradients
- improve S_3 flipping and gradients

- add flipping of B_z

- higher-power photoionizing laser

- gentler RAC-MOT

MSSM and β decay correlations

Profumo, Ramsey-Musolf, Tulin

PRD 75 075017 2017

$C_S + C'_S$ can be 0.001 in MSSM in
1-loop order including mixing

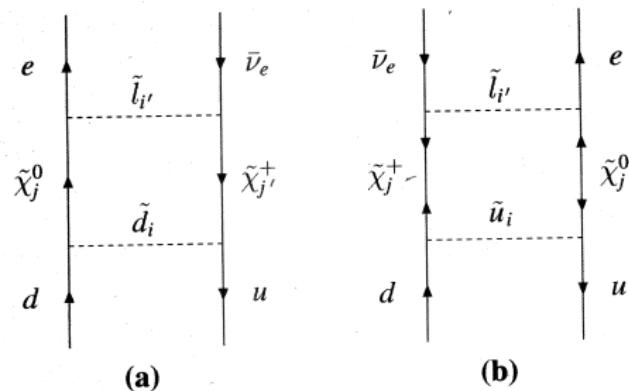


FIG. 2. Feynman diagrams relative to supersymmetric contributions giving rise to anomalous amplitudes in β decay processes.

Include mixing of:

- left and right sfermions (this is where β decay can help; constraints are said to be few)
 - sfamily mixing (already tightly constrained, e.g. by $\mu \rightarrow e \gamma \dots$)
- Effective 4-fermi scalar and tensor couplings are generated that contribute to $\mathbf{b}_{\text{Fierz}}$ and spin correlation observables like \mathbf{B}_ν , as large as 0.001.

nucleon form factors

Herczeg Prog Part Nucl Phys 46 (2001) 413 pointed out need for form factors

$$\langle p | \bar{u} \sigma_{\lambda \mu} d | n \rangle = g_T(q^2) \bar{u}_p \sigma_{\lambda \mu} u_n$$

$$\langle p | \bar{u} d | n \rangle = g_s(q^2) \bar{u}_p u_n$$

2001: “ $0.25 < g_s < 1$ ” depressing to the experimentalist
 g_T related to transverse spin structure function

Bhattacharya, Cirigliano, et al. PRD 85 05412 (2012) first lattice gauge calculations,

$$g_s = 0.8 \pm 0.4, \quad g_T = 1.05 \pm 0.35$$

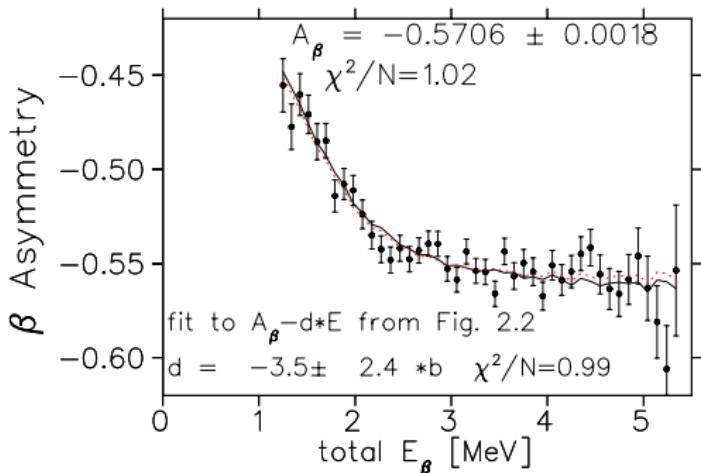
→ (2016) PRD 94 054508

$$g_s = 0.97 \pm 0.12 \pm 0.06, \quad g_T = 0.987 \pm 0.051 \pm 0.020$$

$g_s = 1.02 \pm 0.10$ Gonzalez-Alonso, Camalich PRL 112 042501
 (2014) isospin symmetry



2nd-class currents



“2nd-class” weak interactions would violate isospin symmetry when quarks are combined by QCD into nucleons.
 “Induced tensor” d is near zero in isobaric mirror decay.

This result is complementary to other nuclear β decay (Sumikama PRC 2011) in models where 2nd-class currents change with system (Wilkinson EPJA 2000)

Babar set best 3-generation constraints PRL 2009

$$\tau^- \rightarrow \omega \pi^- \nu_{\tau}$$



Super-ratio

$$A_{\text{obs}}^{\text{SR}}(E_e) = \frac{1-s(E_e)}{1+s(E_e)} = A_{\text{obs}}$$

$$s(E_e) = \sqrt{\frac{r_1^-(E_e)r_2^+(E_e)}{r_1^+(E_e)r_2^-(E_e)}}$$

**Gay, T.J. and Dunning, F.B. Rev. Sci. Instrum. 63 (1992)
1635**

B. Plaster et al. PRC 86 (2012) 055501